Overview and Background	Data 00	Average Treatment Effect 00	Heterogeneity 00000	Policy Targeting	Conclusion

# Peaking Interest: How awareness drives the effectiveness of time-of-use electricity pricing

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Camp Resources XXIV

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Overview and Background ●0○	Data 00	Average Treatment Effect 00	Heterogeneity 00000	Policy Targeting	Conclusion
Overview and Preview of Result	ts				
Overview					

- Goal
  - Using machine learning to estimate heterogeneous treatment effects from TOU electricity pricing & info. provision
  - Meaning? "Under what conditions do consumers change their electricity consumption in response to prices that vary by time of day?"

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#### Heterogeneity

- Why? targeting, understanding mechanisms
- Context: rich dataset from experiment on Irish households
- Problem: multiple testing
- What's needed: parsimonious way to estimate heterogeneity in many dimensions in a robust manner → machine learning

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#### • Average TOU pricing effect: -9% peak consumption

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  - Size of price change doesn't matter
  - Nothing else matters (out of 150+ household characteristics)
- Other findings:
  - Can't reliably predict who will be aware
  - Real-time pricing not necessarily more efficient than TOU

Overview and Background ○○●	Data 00	Average Treatment Effect	Heterogeneity 00000	Policy Targeting	Conclusion
Background on Time-of-Use Pr	icing				

#### What is Time-of-Use Pricing?



Overview and Background	Data ●0	Average Treatment Effect 00	Heterogeneity 00000	Policy Targeting	Conclusion
Experiment					
Experimental	Deta	ils			

- 2009: Households recruited; baseline data collected; pre-trial survey; randomized to treatment/control
- 2010: Treatment period
- 2011: Follow-up survey

	Bi-Monthly Bill / En- ergy Statement	Monthly Bill / Statement	In-Home Display	Load Reduction Incentive	Control
Tariff A	195	216	205	216	0
Tariff B	80	87	72	81	0
Tariff C	222	217	202	213	0
Tariff D	80	87	78	77	0
Control	0	0	0	0	678

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e -		
8		20
~ ]	- Control (No Change)	26

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Overview and Background	Data 0●	Average Treatment Effect 00	Heterogeneity 00000	Policy Targeting 00	Conclusion
Experiment					
Data					

#### • Household Electricity Consumption ( $N \times T \approx 77$ million)

- $N\approx 3,000~{\rm households}$
- $T \approx 26,000$  half-hours each

Overview and Background	Data 0●	Average Treatment Effect 00	Heterogeneity 00000	Policy Targeting	Conclusion
Experiment					
Data					

#### • Household Electricity Consumption ( $N \times T \approx 77$ million)

- $N \approx 3,000$  households
- $T \approx 26,000$  half-hours each
- Survey data: > 150 complete variables on...
  - *Family characteristics*: Employment status, education, social class, household size, #adults, #children, etc.
  - *House characteristics*: age, #rooms, #bedrooms, style, insulation, window glazing, etc.
  - **Appliance & electronics characteristics**: home heating fuel types, water heating fuel types, #immersion heaters, #dishwashers, #washing machines, #tumble dryers, #TVs (by size), #computers, #game consoles, internet access, etc.
  - **Attitudinal/Behavioral**: Attitudes towards energy, environment, etc., expected achievable energy savings, appliance & electronics usage behavior, reasons for participating in the program, etc.
  - Post-experiment survey: questions about experience with program

Overview and Background	Data 00	Average Treatment Effect	Heterogeneity 00000	Policy Targeting	Conclusion

Overview and Background	Data 00	Average Treatment Effect	Heterogeneity 00000	Policy Targeting	Conclusion

Average Treatment Effect

Overview and Background	Data 00	Average Treatment Effect	Heterogeneity 00000	Policy Targeting	Conclusion

- Average Treatment Effect
- e Heterogeneity

Overview and Background	Data 00	Average Treatment Effect	Heterogeneity 00000	Policy Targeting	Conclusion

- Average Treatment Effect
- e Heterogeneity
- Policy Targeting

Overview and Background	Data 00	Average Treatment Effect ●0	Heterogeneity 00000	Policy Targeting 00	Conclusion
Average Treatment Effect					

### Average Treatment Effect

Overview and Background	d Data 00	Average Treatment Effect ⊙●	Heterogeneity 00000	Policy Targeting	Conclusion
Average Treatment Effect					
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#### Difference-in-Differences (All Treatments)

 $\ln(kwh_{i,h,t}) = \beta_h Treatment_{i,h,t} + \alpha_{i,h} + \lambda_{m,h} + \epsilon_{i,h,t}$ 

Overview and Background	Data 00	Average Treatment Effect 0•	Heterogeneity 00000	Policy Targeting	Conclusion
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Overview and Background	Data 00	Average Treatment Effect 00	Heterogeneity	Policy Targeting	Conclusion

### Heterogeneity

Overview and Background	Data 00	Average Treatment Effect 00	Heterogeneity ●0000	Policy Targeting 00	Conclusion
Heterogeneity					

#### Methods: Athey-Imbens & Extensions

Athey & Imbens (2016)

• Estimates CATEs w/ trees ("Conditional" ATE)



#### Extensions in this paper

- Diff-in-diff (vs. "diff")
  - Replace  $Y_i$  with  $\Delta Y_i$
- Multiple treatment groups
  - Allow splitting on treatment



Overview and Background	Data 00	Average Treatment Effect 00	Heterogeneity 0●000	Policy Targeting	Conclusion
Heterogeneity					

### How does Athey-Imbens work? (Simple Version)

 $Y_i$  ... outcome,  $W_i$  ... treatment, p ... share treated  $\left(\frac{n_T}{n}\right)$ 

$$Y_i^* \equiv Y_i \frac{W_i - p}{p(1 - p)} = \begin{cases} Y_i / p & \text{if } W_i = 1\\ -Y_i / (1 - p) & \text{if } W_i = 0 \end{cases}$$

Overview and Background	Data 00	Average Treatment Effect 00	Heterogeneity 0●000	Policy Targeting	Conclusion
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$$\begin{aligned} \frac{1}{n} \sum_{i} Y_{i}^{*} &= \frac{1}{n} \left[ \sum_{i \in \mathcal{S}_{T}} \frac{Y_{i}}{p} + \sum_{i \in \mathcal{S}_{C}} \frac{-Y_{i}}{1-p} \right] = \frac{1}{n} \left[ \sum_{i \in \mathcal{S}_{T}} \frac{Y_{i}}{n_{T}/n} + \sum_{i \in \mathcal{S}_{C}} \frac{-Y_{i}}{n_{C}/n} \right] \\ &= \frac{1}{n_{T}} \sum_{i \in \mathcal{S}_{T}} Y_{i} - \frac{1}{n_{C}} \sum_{i \in \mathcal{S}_{C}} Y_{i} \\ &= LATE \end{aligned}$$

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Intuitively, model  $Y_i^*$  as a flexible function of  $X_i$ :  $E[Y_i^*|X_i] = f(X_i) = "ATE(X_i)"$ 

Overview and Background	Data 00	Average Treatment Effect 00	Heterogeneity ○○●○○	Policy Targeting 00	Conclusion
Heterogeneity Results					

### Heterogeneity Results



Overview and Background	Data 00	Average Treatment Effect 00	Heterogeneity ○○○○●	Policy Targeting	Conclusion
Heterogeneity Results					

#### Aside: Mean Demand Curves, by Period of Day



Heterogeneous Demand

Overview and Background	Data 00	Average Treatment Effect 00	Heterogeneity ○○○○●	Policy Targeting	Conclusion
Heterogeneity Results					

#### Aside: Mean Demand Curves, by Period of Day



- Commonly-used constant elasticity assumption is invalid •
- Real-time pricing not necessarily better (& possibly worse)

Overview and Background	Data 00	Average Treatment Effect 00	Heterogeneity 00000	Policy Targeting	Conclusion

### Policy Targeting

Overview and Background	Data 00	Average Treatment Effect	Heterogeneity 00000	Policy Targeting ●0	Conclusion
Who is likely to be aware?					
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#### Targeting Likely-Aware Households

- Target on awareness?
  - Why? Costs, customer blowback
- Classification problem:  $P(Aware_i = 1|X_i) = f(X_i)$ 
  - Same problem: many variables, multiple testing
  - Solution: Post-selection Lasso for variable selection/elimination

Overview and Background	Data 00	Average Treatment Effect 00	Heterogeneity 00000	Policy Targeting ○●	Conclusion
Who is likely to be aware?					

#### Lasso Post-Selection LPMs on Awareness

	Aware of T	ariff Change	(Indicator)
	LPM	Lasso-Min	Lasso-1SE
Internet Access in Home (Indicator)	0.06	0.06	0.13
Use Internet Regularly (Indicator)	0.02	0.01	
Water Heating Fuel: Oil (Indicator; "none" omitted)	0.05	0.04	
Number of Dishwashers in Home	0.03	0.04	
Number of Desktop Computers in Home	0.02	0.01	
Expect Participating in Trial Will Reduce My Bill (Indicator)	0.05	0.06	
Female Respondent (Indicator)	0.04	0.04	
Social Class: AB (Highest) (Indicator)	-0.02	0.02	
Education: Third (e.g., University) (Indicator)	0.05	0.04	
Info. Treatment: In-Home Display (Indicator; Bi-monthly Bill omitted)	0.05	0.05	
Info. Treatment: Monthly bill (Indicator; Bi-monthly Bill omitted)	0.04	0.05	
Info. Treatment: OLR (Indicator; Bi-monthly Bill omitted)	-0.01		
$R^2$	0.12	0.07	0.03
Adjusted R <sup>2</sup>	0.07	0.07	0.03
Observations	2,328	2,328	2,328
Number of Covariates	123	17	1
Number of Covariates Not Shown	111	6	0
Number of Covariates Significant (5% level)	14 (11.4%)	na	na

Overview and Background	Data 00	Average Treatment Effect 00	Heterogeneity 00000	Policy Targeting	Conclusion
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- Awareness of the TOU pricing is key to effectiveness
  - $\Rightarrow\,$  Awareness not predictable, so focus on information

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CONCIUSION					

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  Awareness not predictable, so focus on information
- Small consumers don't respond (in levels or percentages)
  - $\Rightarrow$  Target larger consumers

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⇒ Information is important

Size of price change doesn't matter

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- Size of price change doesn't matter

Getting prices exactly right isn't as important as getting people to pay attention in the first place

Overview and Background	Data 00	Average Treatment Effect 00	Heterogeneity 00000	Policy Targeting	Conclusion

## Thanks!



### Average Consumption Profiles, by Group & Period





### Average Consumption Profiles, by Group & Period





### Average Consumption Profiles, by Group & Period



#### Balance Checks: t-tests

	Variable	Control Mean	Treatment Mean	t-statistic	p-value
	Unbalanced Variables ( $\alpha < 0.05$ )				
1	Employment status: Retired (Indicator)	0.38	0.31	3.40	0.001
2	Number of Large Televisions (21+ inch)	1.19	1.31	-3.36	0.001
3	Number of Electronics	3.74	4.04	-3.03	0.003
4	Age Group: 65+ (Indicator)	0.28	0.23	2.79	0.01
5	Has Children Under 15 in Home (Indicator)	0.23	0.28	-2.78	0.01
6	Number of Residents	2.60	2.76	-2.65	0.01
7	Social Class: AB (Highest) (Indicator)	0.12	0.15	-2.58	0.01
8	Education: Primary only (Indicator)	0.15	0.11	2.51	0.01
9	Baseline Average Consumption (Night Hours)	0.14	0.15	-2.42	0.02
10	Internet Access in Home (Indicator)	0.66	0.71	-2.24	0.02
11	Number of Desktop Computers	0.48	0.53	-2.18	0.03
12	Number of Children Under 15 in Home	0.43	0.52	-2.11	0.04
13	Housing Status: Own with Mortgage (Indicator)	0.35	0.40	-2.09	0.04
14	Others in Household Use Internet Regularly (Indicator)	0.53	0.57	-2.01	0.04
	Selected Balanced Variables ( $\alpha \ge 0.05$ )				
15	Baseline Average Consumption (Peak Hours)	0.42	0.44	-1.85	0.07
16	Number of Adults in Home	2.16	2.24	-1.74	0.08
17	Cook stove type: Electric (Indicator)	0.72	0.69	1.62	0.10
18	Number of Laptop Computers	0.65	0.71	-1.61	0.11
19	Baseline Average Consumption (Day Hours)	0.29	0.30	-1.56	0.12
20	Unemployed, not seeking job (Indicator)	0.03	0.04	-1.52	0.13
21	Home Heat: Solid Fuel (Indicator)	0.29	0.26	1.46	0.14
22	Interested in changing energy use for environment*	1.38	1.34	1.41	0.16
23	Female (Indicator)	0.47	0.50	-1.02	0.31
24	Education: Secondary to Certificate (Indicator)	0.16	0.17	-0.86	0.39
25	Satisfied with billing frequency*	2.84	2.86	-0.47	0.64
	Observations	3,006			
	Number of Variables Tested	122			
	Number of Variables Not Shown	97			
	Number of Variables Significant (5% level)	14			
	Share of of Variables Significant (5% level)	11.5%			

Return to main

### Balance Checks: LPM

	Dependent variable:	
	Treated (Indicator)	
Baseline Average Consumption (Peak Hours)	0.03	
· · · · /	(0.07)	
Baseline Average Consumption (Night Hours)	0.14	
	(0.15)	
Baseline Average Consumption (Day Hours)	-0.09	
	(0.12)	
Number of Large Televisions (21+ inch)	0.02**	
	(0.01)	
Age Group: 65+ (Indicator)	0.13	
	(0.11)	
Number of Adults in Home	0.01	
	(0.01)	
Internet Access in Home (Indicator)	0.01	
	(0.02)	
Number of Desktop Computers in Home	0.01	
	(0.02)	
Others in Household Use Internet Regularly (Indicator)	-0.003	
	(0.02)	
Cook stove type: Electric (Indicator)	-0.13**	
	(0.06)	
Observations	3,006	
$R^2$	0.03	
Adjusted R <sup>2</sup>	-0.01	
Number of Covariates	109	
Number of Covariates Not Shown	100	
Number of Covariates Significant (5% level)	2	
Share of Covariates Significant (5% level)	1.8%	



### Placebo test for TOU pricing: Weekends & Holidays



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#### Balance Tests & Diagnostics

#### Diff-in-Diff (Individual Treatments)



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Balance Tests & Diagnostics

#### Checking for pre-trends in peak consumption



Peaking Interest

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Tree Sensitivities

#### Robustness Check: Propensity Tree



Tree Sensitivities

#### Robustness Check: "Honest" Tree



Appendix 0000000000000

Heterogeneous Demand Curves

#### Heterogeneous Demand Curves



Appendix ○○○○○○○○●○

Extension - Multiple Treatment Groups

#### Extension - Multiple Treatment Groups

For each control observation i and treatment  $m \in \{1, ..., M\}$ , generate a new pseudo-observation  $i_m$  with

$$\begin{array}{rcl} Y_{i_m} & \equiv & Y_i \\ X_{i_m} & \equiv & X_i \\ W_{i_m} & \equiv & W_i \; (=0) \end{array}$$
  
For  $m' \in \{1,...,M\}$   $W_{i_m}^{m'} & \equiv & \begin{cases} 1 & \text{for } m' = m \\ 0 & \text{for } m' \neq m, \end{cases}$ 

for a total of  $M \times n_C$  control observations, replacing the  $n_C$  original ones

Appendix ○○○○○○○○○

Extension - Multiple Treatment Groups

#### Extension - Multiple Treatment Groups

#### Transformed LATE:

$$\begin{aligned} \frac{1}{n_T} \sum_{i \in \mathcal{S}_T} Y_i - \frac{1}{M \times n_C} \sum_{i \in \tilde{\mathcal{S}}_C} Y_i &= \frac{1}{n_T} \sum_{i \in \mathcal{S}_T} Y_i - \frac{1}{M \times n_C} M \sum_{i \in \mathcal{S}_C} Y_i \\ &= \frac{1}{n_T} \sum_{i \in \mathcal{S}_T} Y_i - \frac{1}{n_C} \sum_{i \in \mathcal{S}_C} Y_i \\ &= \hat{\tau}, \end{aligned}$$

which is the same as the LATE estimate of the untransformed data.

Return