

Age-Adjusted Value of Statistical Life: Evidence from Automobile Purchase Decisions

James O'Brien
Georgetown University
jho8@georgetown.edu

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Motivation:

Age variation in the VSL from vehicle choice

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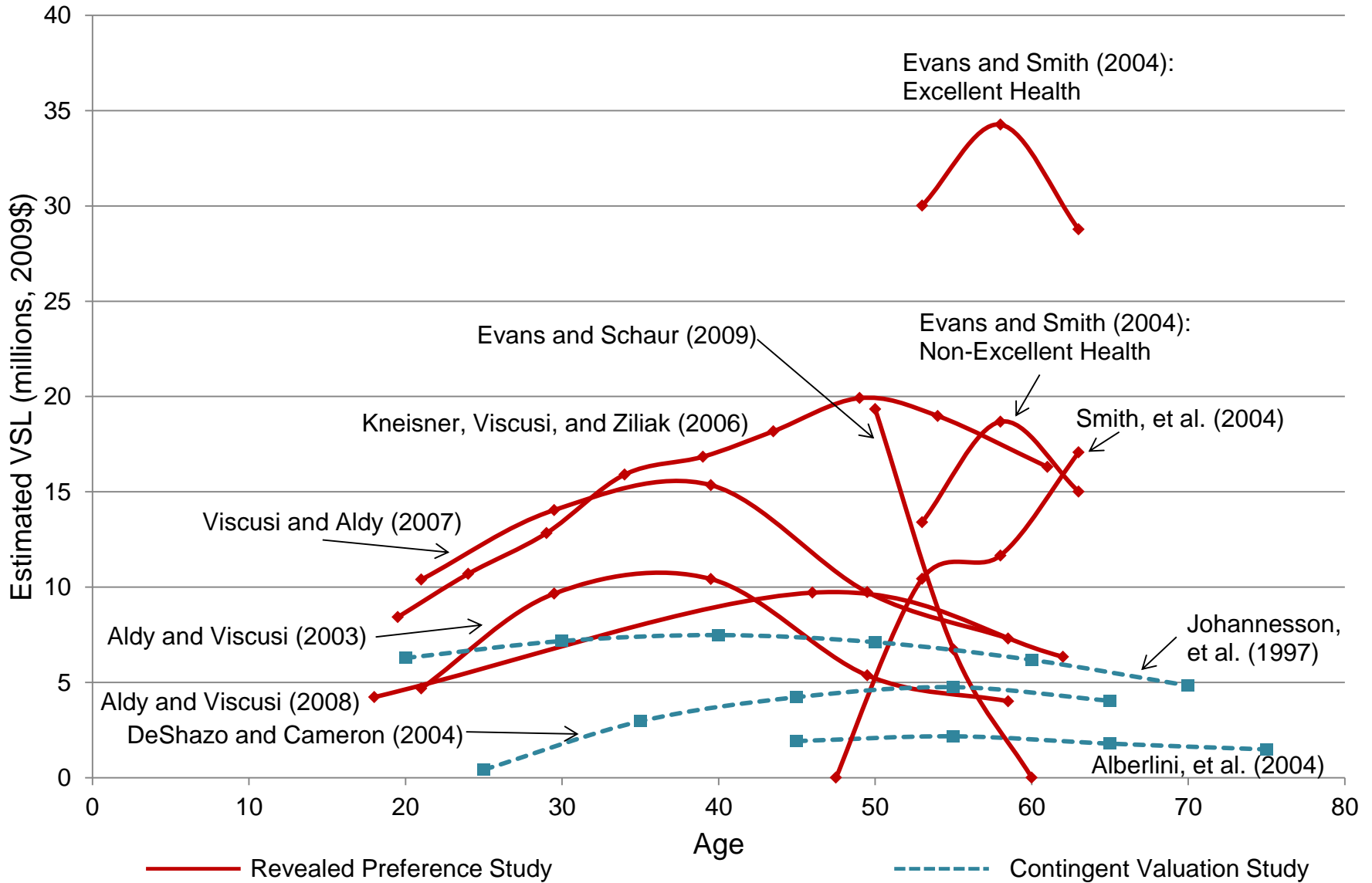
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Separately observe the effects of cost and risk

Estimate VSL in a different context:

Possibly more applicable to road and vehicle safety regulations

Selected Age-VSL Results in Recent Literature



Multinomial Vehicle Choice Model

Standard McFadden (1974) MNL framework:

Consumers obtain utility from vehicle attributes:

$$U_i^n = \sum_c \beta_{1c} risk_i^c * I_c(age_n) + \sum_c \beta_{2c} \frac{cost_i}{income_n} * I_c(age_n) + X_i^n \gamma + \varepsilon_i^n$$

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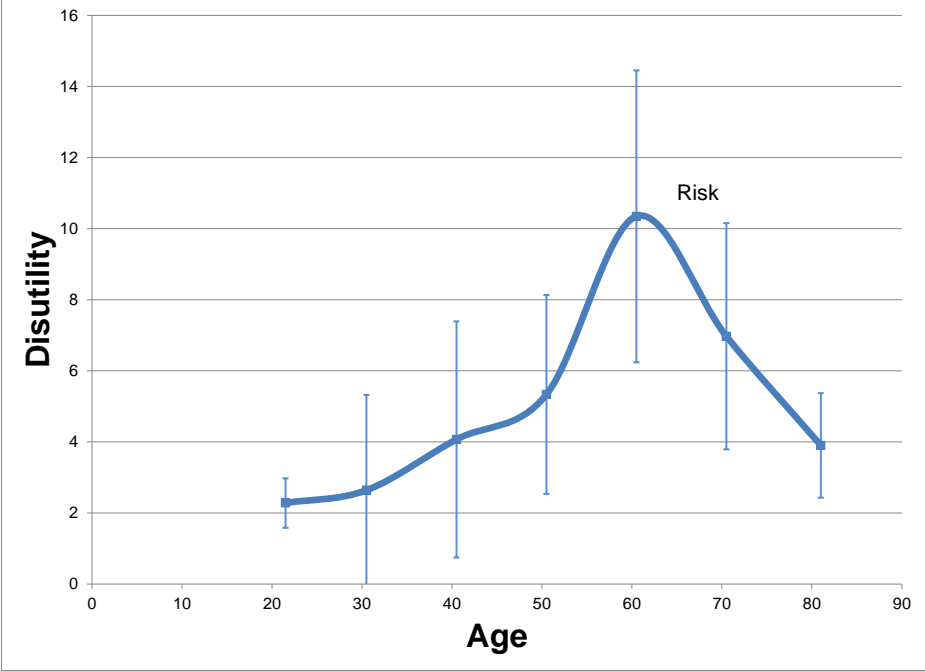
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Value of Statistical Life

$$-\frac{\partial cost}{\partial risk^c} = VSL^c = \frac{\beta_{1c}}{\beta_{2c}} * \overline{income}^c$$

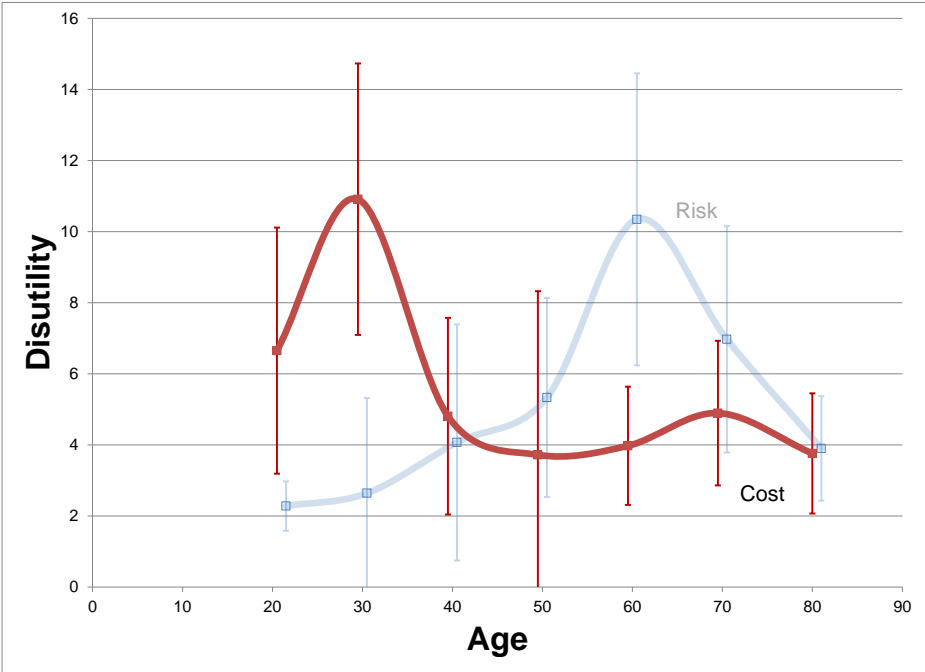
Multinomial Results

Risk Coefficients



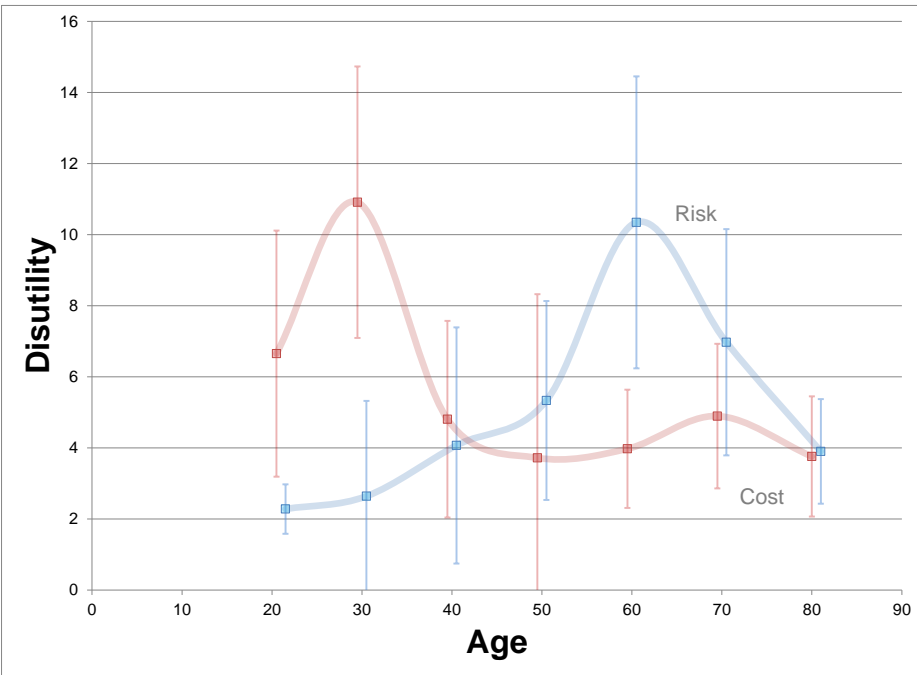
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Cost Coefficients

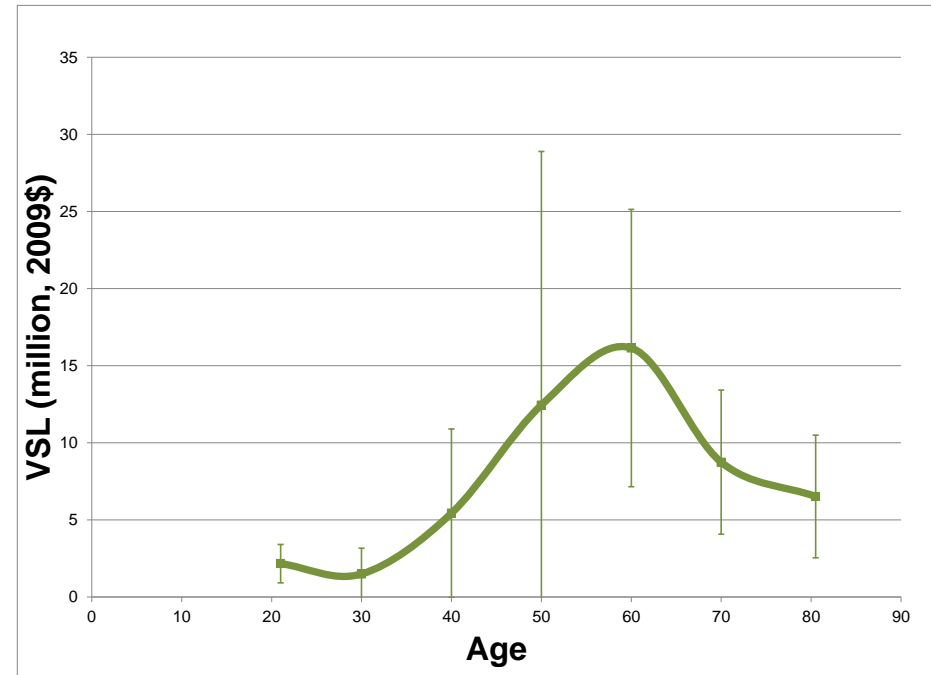


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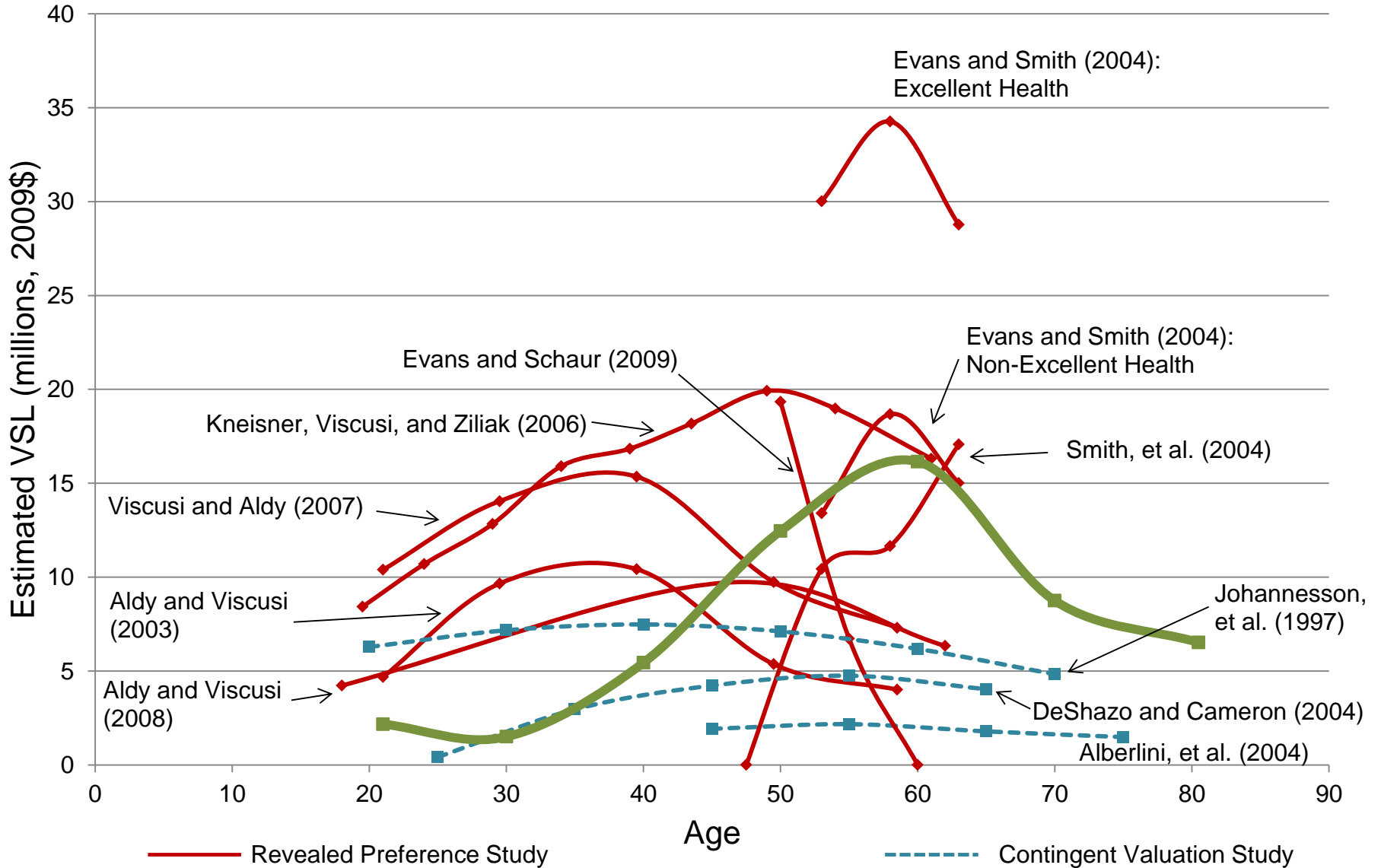
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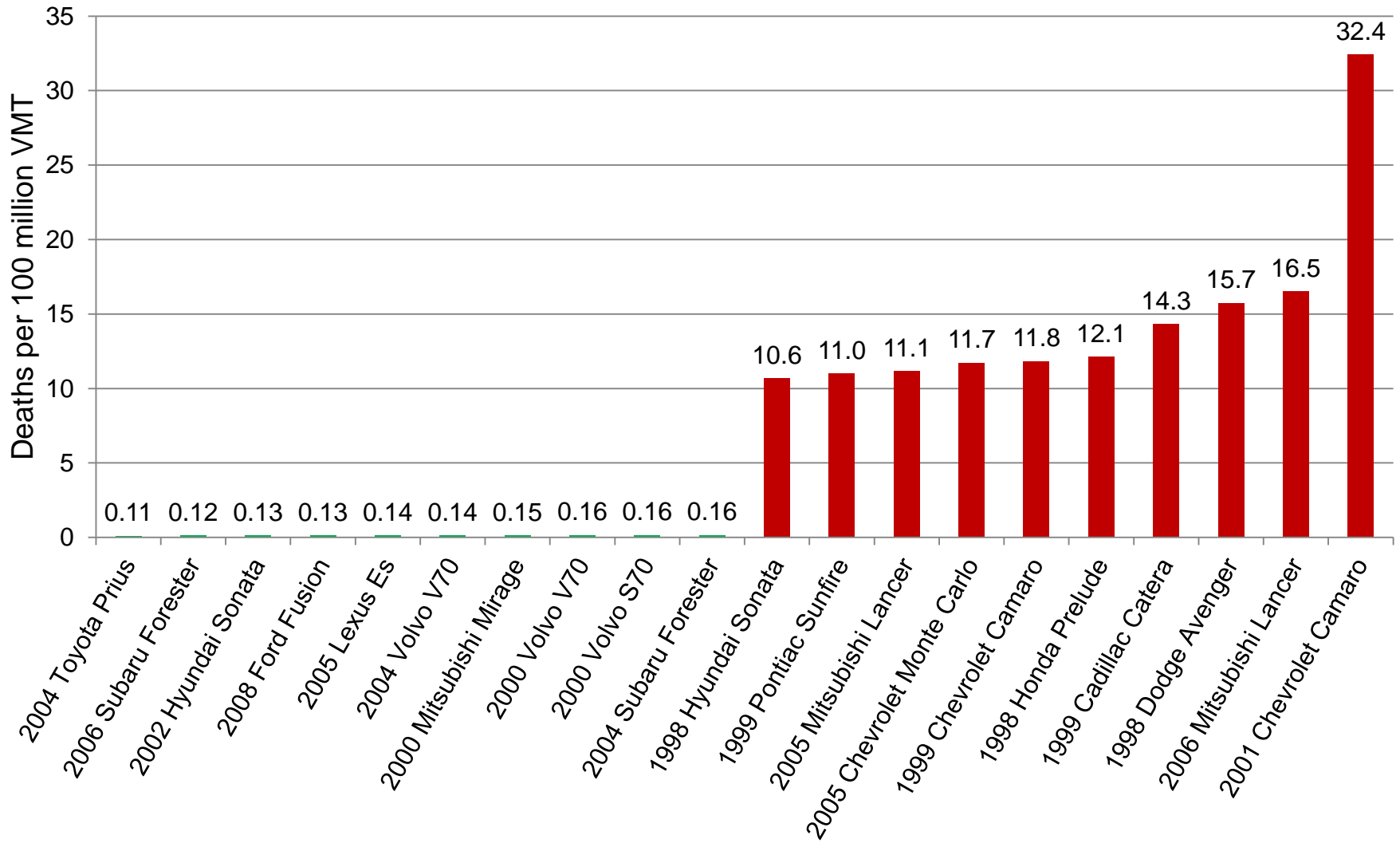
VSL Estimates



Selected Age-VSL Results in Recent Literature



Endogenous Car Choices



Accounting for Driver Behavior

- i. Estimate relative driver effects based on crash test results and single-vehicle fatalities ($Y_{i,c}$)

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$$E[Y_{i,c}] = \alpha_v \lambda_c X_i$$

The diagram illustrates the components of the expected value of single-vehicle fatalities. The equation $E[Y_{i,c}] = \alpha_v \lambda_c X_i$ is shown. Three red arrows point from labels below to the terms in the equation: 'Driver effects' points to α_v , 'Age cohort effects' points to λ_c , and 'Crash test results' points to X_i .

Accounting for Driver Behavior

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$$E[Y_{i,c}] = \alpha_v \lambda_c X_i$$

Driver effects

Age cohort effects

Crash test results

- ii. Adjust overall deaths per mile ($Z_{j,c}$) for each alternative based on the $\hat{\alpha}$'s

(example: find the fatality risk in a Camaro if driven by a Prius driver)

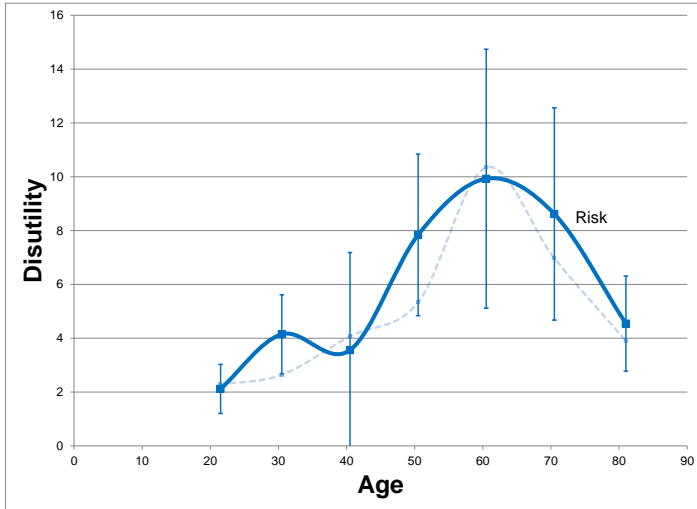
$$\text{Counterfactual deaths per mile} \rightarrow \widetilde{risk}_{j,c} \Big|_i = \frac{\alpha_i risk_{j,c}}{\hat{\alpha}_j}$$

Counterfactual deaths per mile

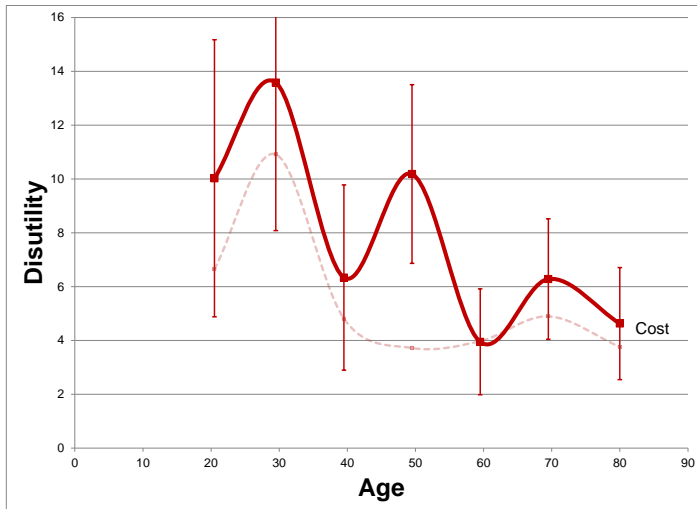
Deaths per mile in data

Adjusted MNL Results

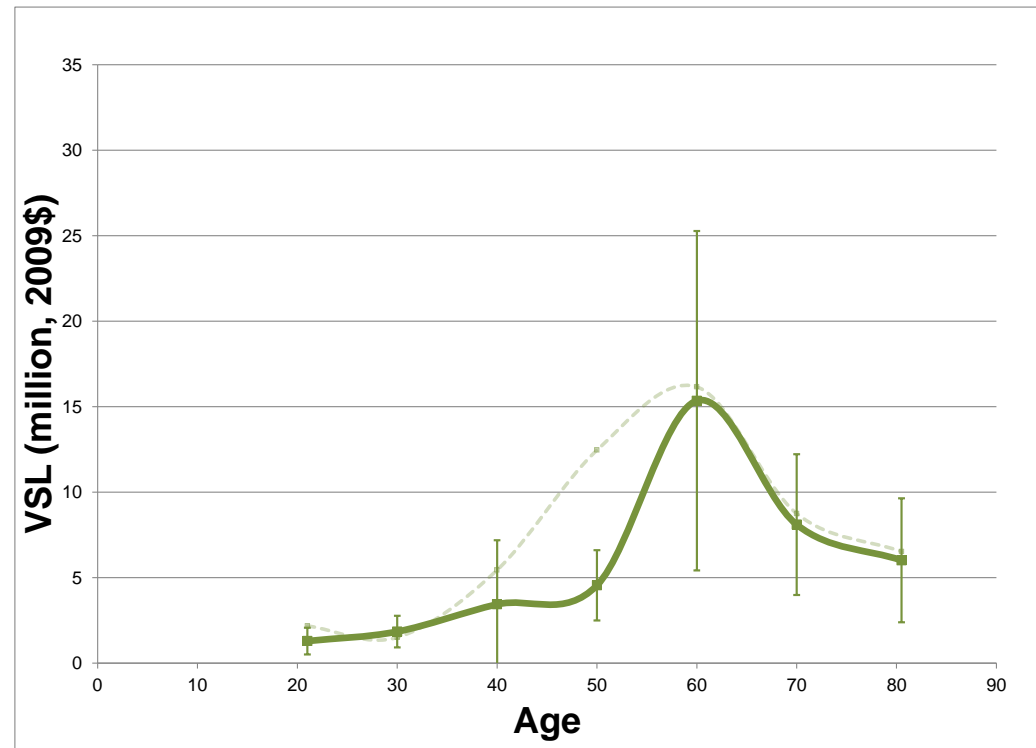
Risk Coefficients



Cost Coefficients



VSL Estimates



Alternative Approach: Control Function

- Problem is due to the correlation between between $risk_i^c$ and ε_i^n

$$U_i^n = \sum_c \beta_{1c} risk_i^c * I_c(age_n) + \sum_c \beta_{2c} \frac{cost_i}{income_n} * I_c(age_n) + X_i^n \gamma + \varepsilon_i^n$$

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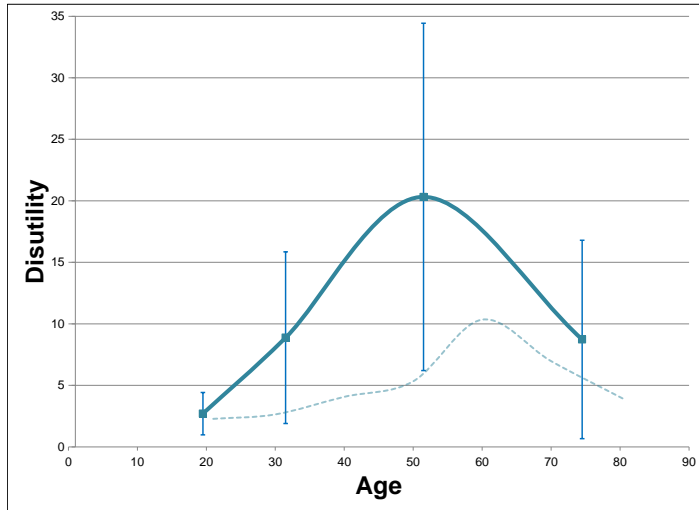
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- Include consistent estimates of ε_{ic}^{1n} as **additional regressors**

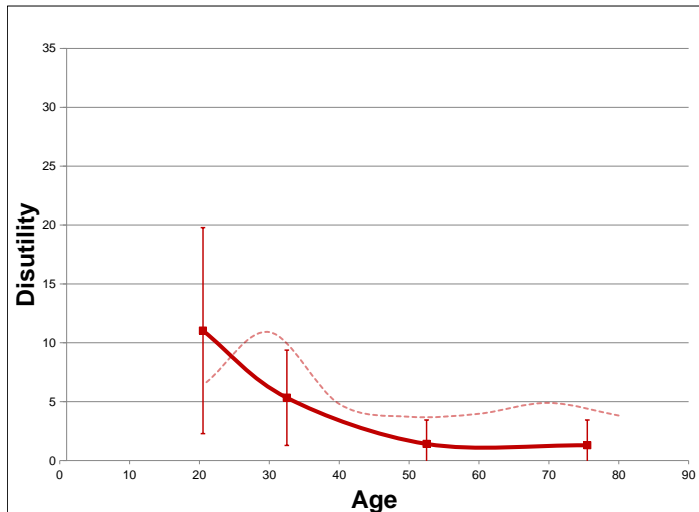
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Control Function Results

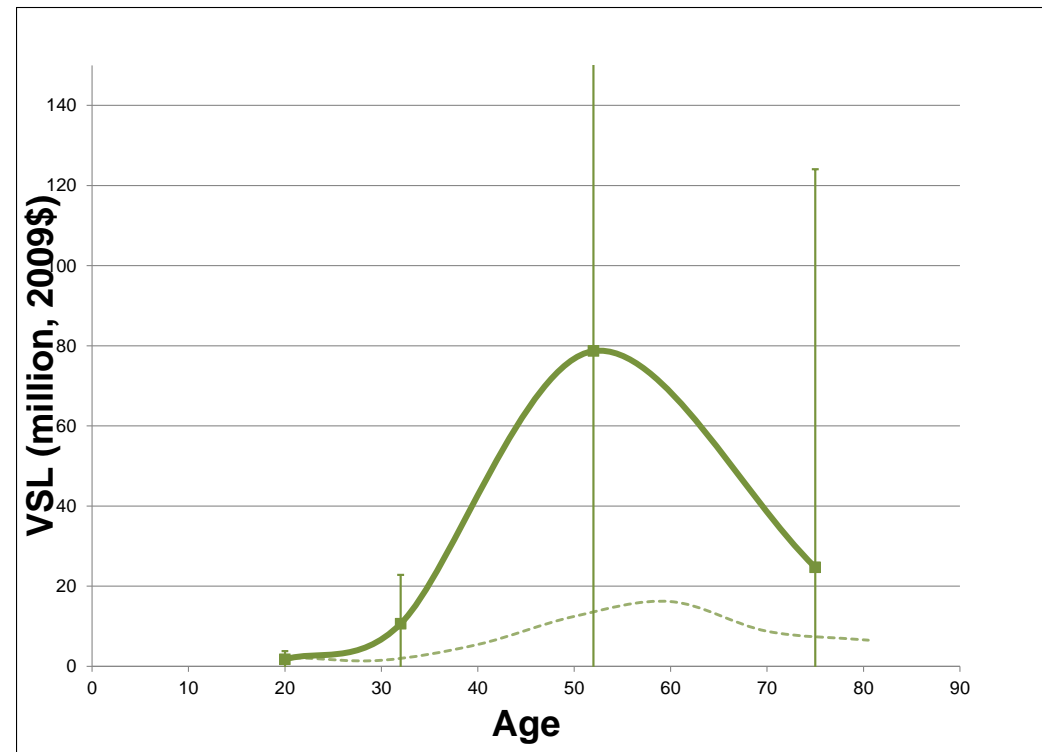
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VSL Estimates

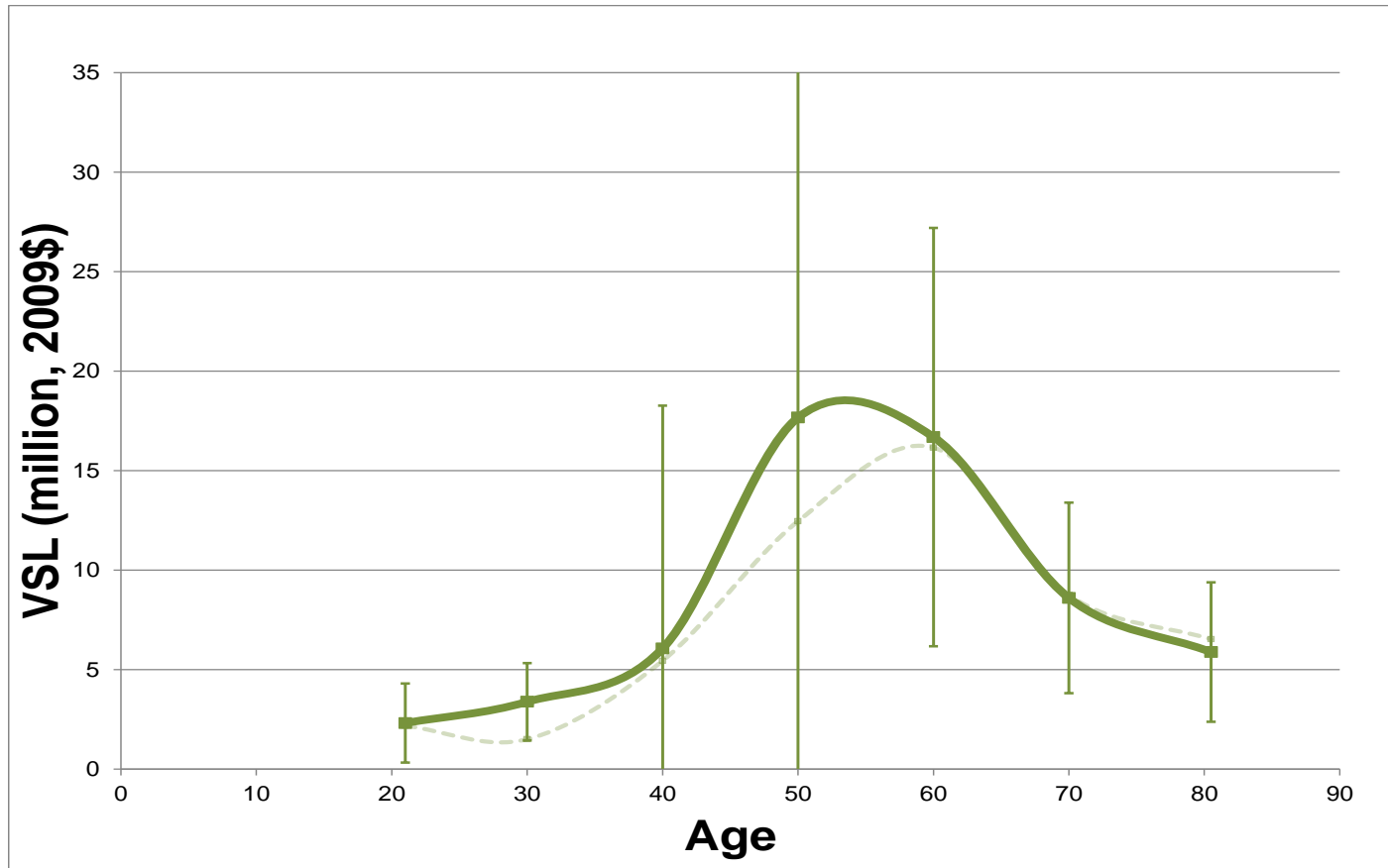


Conclusion

- Extend range of revealed preference evidence
- No evidence of a “senior discount” *per se*
- Corroborate inverted-U shape
- Risk adjustments and Control Functions are *very* preliminary

Appendix 1

VSL of Households with No Children



Appendix 2: Control Function Details

- Bias arises because of a correlation between $risk_i^c$ and ε_i^n

$$\varepsilon_i^n = \sum_c \varepsilon_{ic}^{1n} * I_c (age_n) + \varepsilon_i^{2n}$$

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- Assume ε_{ic}^{1n} and μ_i^c are correlated and jointly normal
- Observe that:

$$\varepsilon_{ic}^{1n} \equiv E[\varepsilon_{ic}^{1n} | \mu_i^c] + \widetilde{\varepsilon}_{ic}^{1n} = \varphi_c \mu_i^c + \rho_c \eta_c$$

parameters ←

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parameters

- Sub into utility function, and model is purged of endogeneity

$$U_i^n = \sum_c \beta_{1c} risk_i^c * I_c(age_n) + \sum_c \beta_{2c} \frac{cost_i}{income_n} * I_c(age_n)$$

$$+ X_i^n \gamma + \sum_c \varphi_c \widehat{\mu}_i^c * I_c(age_n) + \sum_c \rho_c \eta_c + \varepsilon_i^{2n}$$

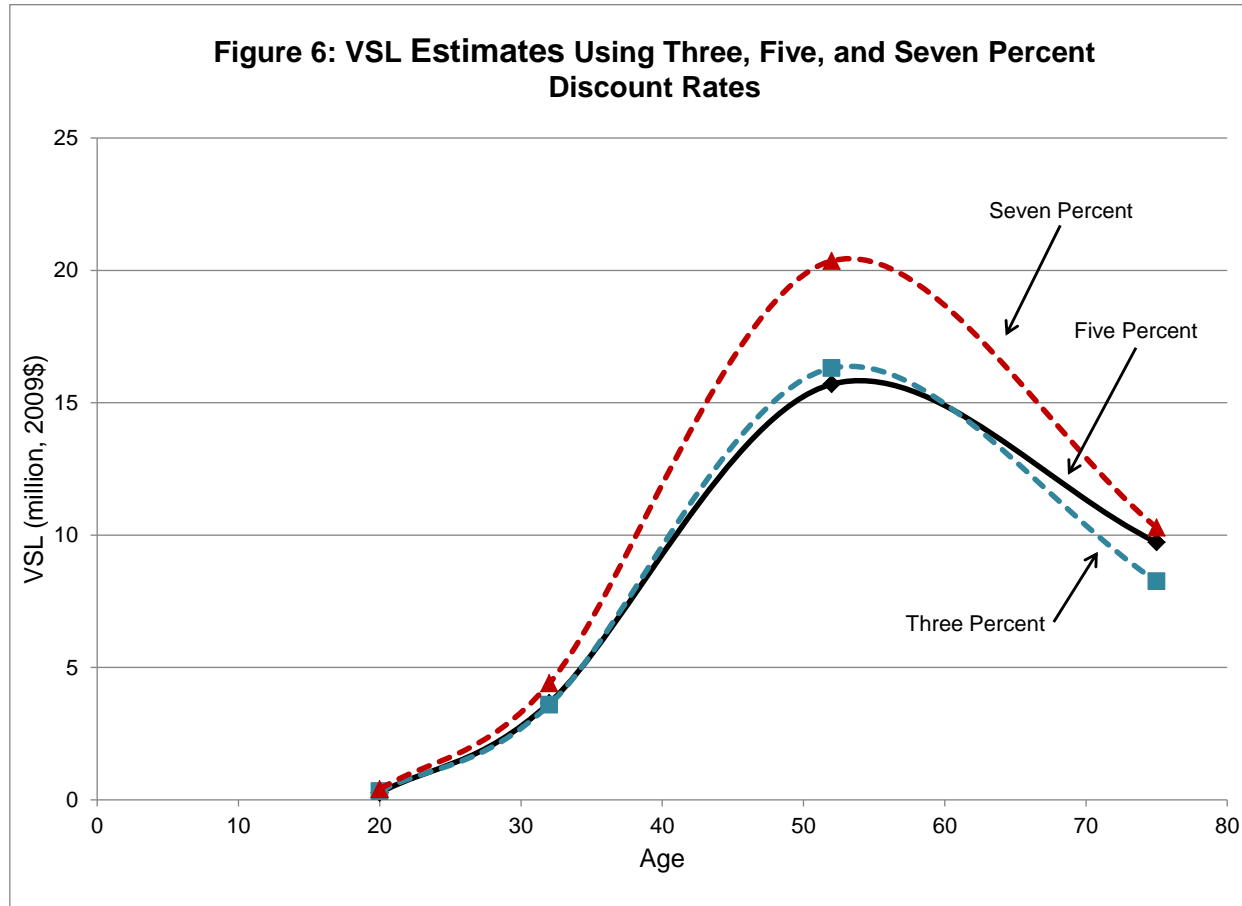
Appendix 3: Other MNL Covariates

Other covariates

Engine Displacement	0.13 [†]
	(0.08)
Cylinders	-0.07
	(0.05)
Cylinder*Pickup	0.31 [†]
	(0.17)
Passenger Volume	0.24*
	(0.05)
Luxury Brand	-0.38*
	(0.10)
Gross Vehicle Weight	-0.01
	(0.05)
Imported	-0.05
	(0.06)
Model Year 2003-2005	0.56*
	(0.06)
Model Year 2006-2008	1.39*
	(0.08)
Class specific constants	Yes

Appendix 3

Effects of Various Discount Rates



Mortality and Age

Clean Air Act Amendments

237,100 Annual Deaths



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Seniors: 173,864
(73 percent)

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Rearview Backup Cameras

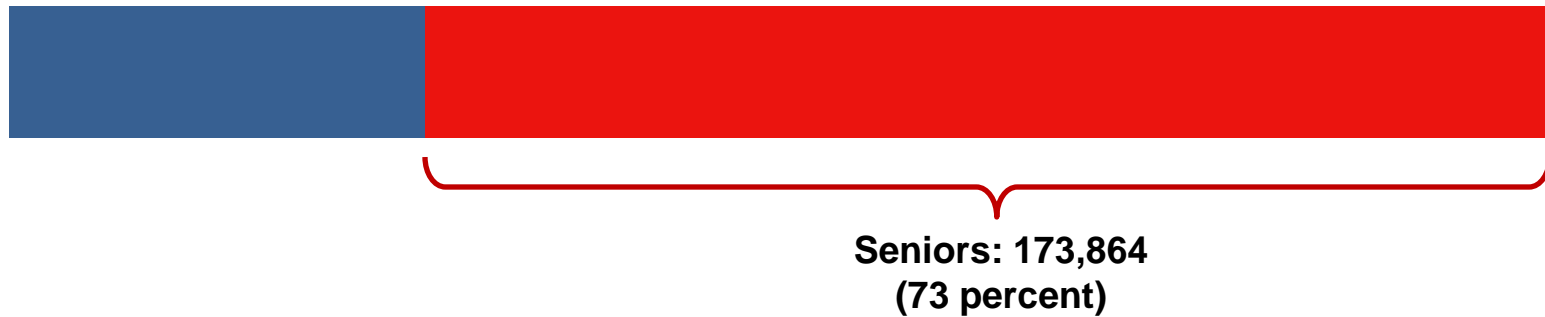
112 Annual Deaths



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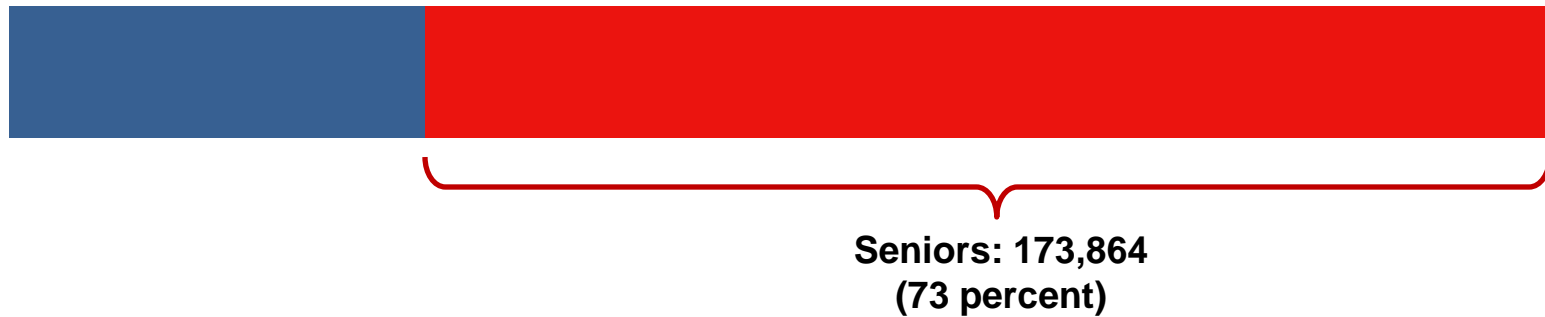
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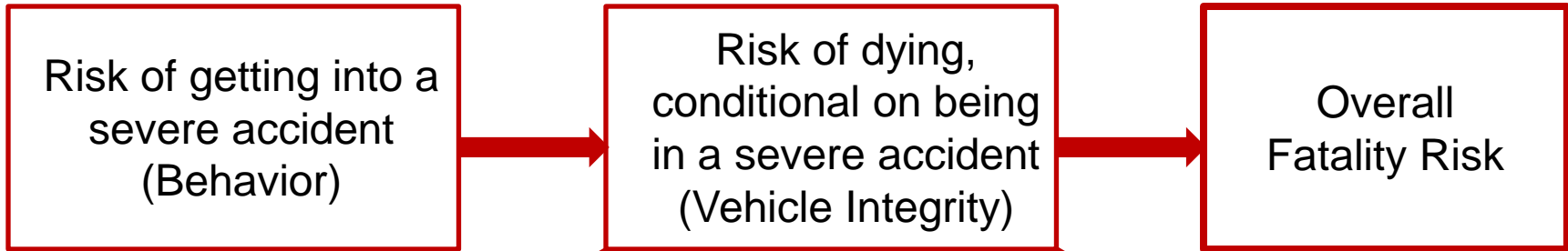


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Crash Test Results



Relative Driver Effects

Vehicle Class	Alpha
Full size	1.23* (0.08)
Compact	0.82* (0.07)
Standard	1.11* (0.05)
Mini	1.55 (0.42)
Pickup	2.48* (0.1)
SUV	1.22* (0.05)
Van	1.24* (0.06)

n 10,360

Significant at the five (*) and ten (†) percent level. Values shown are incident rate ratios relative to economy class vehicles. Age cohort fixed-effects and crash-test coefficients are not shown.

First Stage Results:

Dependent Variable: Deaths per Mile (for Relevant Cohort)

	Age Cohort				
	Overall	Age 18 to 34	Age 35 to 49	Age 50 to 64	Age 65 to 85
	(1)	(2)	(3)	(4)	(5)
Front Head Injury	0.51† (0.29)	2.57 (2.38)	0.19 (0.46)	0.72* (0.29)	3.02* (0.93)
Front Chest Injury	24.86* (8.30)	67.18 (60.41)	26.49* (11.70)	8.61 (6.88)	84.77* (24.50)
Side Head Injury	-0.06 (0.11)	-2.95* (0.83)	-0.31 (0.20)	-0.16 (0.12)	-1.06* (0.39)
F-stat for crash-test variables	12.73	6.746	4.044	4.864	16.35
n	1,381	1,142	873	822	822
Adj. R Squared	0.217	0.112	0.160	0.175	0.138

Note: Other controls: curb weight, tire size, passenger volume, number of cylinders, engine displacement, and indicators for imported, luxury, vintage, and class. Significant at the 5 percent (*) or 10 percent (†) level.